

A Forecasting Methodology as Applied to Rubber Prices

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The paper illustrates a statistical approach using Box and Jenkins' technique to forecast RSS 1 and RSS 2 prices. The technique developed begins with a generalised forecasting model followed by model specification namely identification, estimation and diagnostic checking.

A number of forecasting techniques have been developed depending upon the nature of the variable to be forecast and the purpose of the forecast. In this paper a technique developed by G.E.P. Box and G.M. Jenkins is used as a method to forecast the prices of two grades of rubber – RSS 1 and RSS 2.

There are two main advantages of Box and Jenkins method. First, using the traditional approach one selects arbitrarily a specific forecasting model. For example, in estimating monthly rubber price one may choose double exponential smoothing model when in fact mixed autoregressive moving average (ARMA) model would be more appropriate. Box and Jenkins' methodology starts with a broad, generalised model which takes all possible separate model combinations of moving average and autoregressive models. Using this broad model the forecaster rationally comes to the appropriate specific model. Second, the specific form of a given model has traditionally been the result of a trial-and-error procedure rather than a rational structured approach to the determination of a specific model. Box and Jenkins' structured approach eliminates various hit-and-miss tactics^{1,2}.

The Generalised Model

Time series data can be categorised as stationary and non-stationary data (Figures 1 and 2). Most are generated by a stochastic process. With a time dependent phenomenon and many unknown factors it is not possible to write a deterministic model³.

Stationary models are based on the assumption that the process remains in equilibrium about a constant mean level. Suppose we have a stationary series having mean μ and the observations $Z_t, Z_{t-1}, Z_{t-2}, Z_{t-3}, \dots$ are taken at equal intervals. We define $a_t, a_{t-1}, a_{t-2}, \dots$ as 'white noise' or random shocks to the system. Then there are two ways to model the series as an autoregressive (AR) model; and, as a moving average (MA) model.

An autoregressive model can be expressed as:

$$\bar{Z}_t = \phi_1 \bar{Z}_{t-1} + \phi_2 \bar{Z}_{t-2} + \dots + \phi_p \bar{Z}_{t-p} + a_t \quad \dots 1$$

or using backshift operator B , we can write Equation 1 as:

$$\phi(B)\bar{Z}_t = a_t \quad \dots 2$$

where $\phi(B) = 1 - \phi_1 B - \phi_2 B^2 - \dots - \phi_p B^p$;

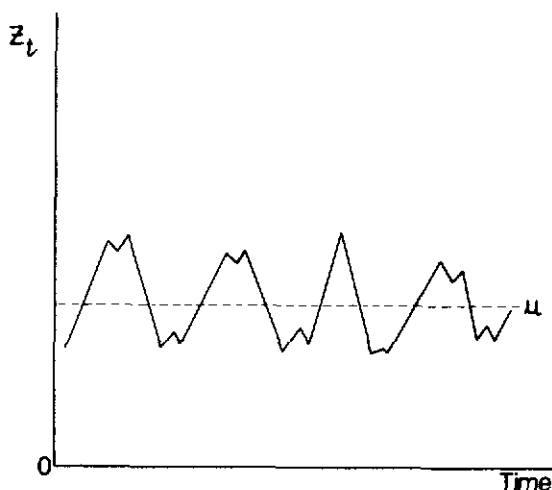


Figure 1. Stationary series.

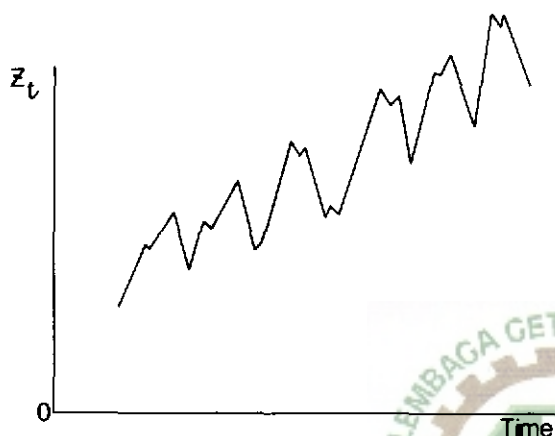


Figure 2. Non-stationary series.

$$a_t \sim NI(0, \sigma^2) \text{ and } \bar{Z}_t = \bar{Z}_t - \mu$$

Sometimes a current deviation from the mean period t is made linearly dependent on all prior deviations back to period $(t-q)$. Therefore, the current deviation can be expressed as a linear function of the 'white noise' to the system. The model, called a moving average model can be expressed as:

$$\bar{Z}_t = a_t - \theta_1 a_{t-1} - \theta_2 a_{t-2} - \dots - \theta_q a_{t-q} \dots 3$$

$$\text{or } \bar{Z} = \theta_q(B)a_t \\ a_t \sim NI(0, \sigma a^2)$$

Almost all of the stochastic or deterministic time series encountered in practice exhibit behaviour suggestive of non-stationarity. Thus, a forecaster should not restrict himself to either an autoregressive model or a moving average model. He should begin with a preliminary model which allows for stochastic and deterministic trend characteristics, non-seasonality and seasonality. The appropriate preliminary model to start with is an autoregressive integrated moving average model of the form:

$$\phi_p(B)(1-B)^d(1-B^s)^D \bar{Z}_t = \theta_p + \theta_q(B)a_t \dots 4$$

$$\text{where } \theta_p = (1 - \phi_1 - \phi_2 - \dots - \phi_p) \mu \\ d = \text{amount of regular differencing}$$

$$s = \text{length of a season}$$

$$\phi_p(B) = 1 - \phi_1 B - \dots - \phi_p B^p$$

$$\theta_q(B) = 1 - \theta_1 B - \theta_2 B^2 - \dots - \theta_q B^p$$

$$D = \text{amount of seasonal differencing}$$

$$\theta_p = \text{represents a deterministic trend constant. Since most of the time series data are generated stochastically, the value of } \theta_p \text{ is normally set equal to zero.}$$

Sometimes Z_t is in the form of logarithm or power transformation. This is to induce constant amplitude in the series over time so that the residuals from the fitted model will have a constant variance. By appropriately choosing certain levels of p , d , q and D , one can obtain an autoregressive model, moving average model or a combination of these.

For example, suppose that a particular series was generated stochastically, it was differenced and was found to arrive at stationarity at $d = 0$, $s = 4$, and $D = 1$. It was also identified that the model was an AR model of the second order, such that $p = 2$, $q = 0$, then our mathematical model, Equation 4 will be:

$$\phi 2B (1-B)^0 (1-B^4)^1 \bar{Z}_t = \theta_0(B) a_t \quad \dots 5$$

From the previous definition, we see that $\phi 2(B) = 1 - \phi_1 B - \phi_2 B^2$ and $\theta_0(B) = 1$. Hence Equation 5 becomes:

$$(1 - \phi_1 B - \phi_2 B^2)(1 - B^4) \bar{Z}_t = a_t \quad \dots 6$$

Expanding

$$(1 - \phi_1 B - \phi_2 B^2 - B^4 + \phi_1 B^5 + \phi_2 B^6) \bar{Z}_t = a_t \quad \dots 7$$

then we can obtain:

$$Z_t = \phi_1 Z_{t-1} + \phi_2 Z_{t-2} + Z_{t-4} - \phi_1 Z_{t-5} - \phi_2 Z_{t-6} + a_t \quad \dots 8$$

Methodology

The identification of a tentative model or set of models from the general class in Equation 4 requires prior knowledge of the data pattern and the plots of sample autocorrelation and partial autocorrelation functions. The plots of autocorrelation and partial autocorrelation functions are the main indicators for identifying a model because each model has a different pattern of plot. A stationary series is required for identification because the theoretical autocorrelation and partial autocorrelation of stationary series have distinct patterns for various models. Thus, any non-stationary series must go through regular and/or seasonal differencing process until the series becomes stationary. The determination of seasonal length(s) can be made by looking at a plot of the series and where it is not easy to identify the seasonal length(s), one should try various values of s .

For each differencing pattern specified by d , D and s , Box and Jenkins calculate sample autocorrelation function, r_k of lag k as:

$$r_k = \frac{\sum_{t=1}^{n-k} (Z_t - \bar{Z})(Z_{t-k} - \bar{Z})}{\sum_{t=1}^n (Z_t - \bar{Z})^2} \quad \dots 9$$

and the theoretical autocorrelation function, ρ_k ;

$$\rho_k = \frac{E(Z_t - \mu)(Z_{t-k} - \mu)}{\sigma^2 Z^2} \quad \dots 10$$

For the autoregressive model of order k for example, there exists an autocorrelation function ρ_j such that:

$$\rho_j = \phi_{k1} \rho_{j-1} + \dots + \phi_{k(k-1)} \rho_{j-k} + 1 + \phi_{kk} \rho_{jk}, \quad j = 1, 2, 3, \dots, k \quad \dots 11$$

where ϕ_{kk} is the last coefficient.

This will lead to Yule-Walker Equation⁴ which may be written in matrix form as:

$$P_k \phi_k = \rho_k \quad \dots 12$$

The quantity ϕ_{kk} regarded as a function of lag k is the partial autocorrelation function. The estimates of partial autocorrelations as shown by Quenouille⁵, of order $p + 1$ and higher are approximately independently distributed with variance:

$$\text{Var}(\phi_{kk}) = \frac{1}{n}; k \geq p + 1$$

where n = number of observation.

$$\text{S.E.}(\phi_{kk}) = \frac{1}{\sqrt{n}} \quad \dots 13$$

Generally, the theoretical autocorrelation function of the AR model will tend

to damp off slowly as k increases. Meanwhile the theoretical autocorrelation function of the MA model is evidenced by Spikes in ρ_k for a particular k . In contrast, the partial autocorrelation function of the AR model drops quickly to zero after k lags, while the partial autocorrelation for the MA model tails off slowly as k increases⁶.

Once a model has been identified, both ϕ_p and θ_q can be estimated by minimising the sum of squares residual term $[E(Z_t - \hat{Z}_t)^2 = \sum a_t^2]$, where \hat{Z}_t is the estimated value of period t . This is done by using a non-linear least square estimation.

The final stage for model determination is the diagnostic checking. This involves the examination of residuals a_t . If the model is adequate these residuals will be normally and independently distributed with mean zero and constant variance, $\sigma^2 a$, (i.e. $a_t \sim NI(0, \sigma^2 a)$). Otherwise the residual autocorrelations should be re-examined, for potential improvement of the model, and the process of identification, estimation and diagnostic checking will continue until an adequate model has been found.

Case Study

This section presents rubber price data for RSS 1 and RSS 2 for the period 1970–81. The patterns of the original data are shown in Figure 3. Each series appears to follow a basic pattern of slow long-run growth with no seasonal fluctuation. Two irregular points appear in each series, in January 1974 and February 1980. A simple explanation would be that during that particular time the demand for natural rubber increased tremendously, but the supply of natural rubber was inelastic. Therefore, when the demand increased suddenly, the price would increase to a much higher level than the

equilibrium price, but when the supply increased or the demand decreased with close substitutes, the price decreased.

Further, investigation of the data reveals that the non-constancy of error variance exists. As the yearly price average increases the error variance increases. Therefore, the original data need transformation to ensure homoskedasticity. The transformation function chosen is $Z_t = \sqrt{Y_t}$.

Identification. Each of the original series indicates that it has an increasing long-term trend. Therefore, each of the series needs at least one degree of regular differencing. Figure 4 shows the results of the first degree of regular differencing for RSS 1 and RSS 2. The two plots suggest that the series have achieved their stationarity. Their autocorrelation and partial autocorrelation in Figures 5, 6 and 7 suggest the more suitable application of the ARMA model. A general ARMA model is ARMA(p, d, q). Having $d = 1$ and varying p and q from 1 to 3 (i.e. $p = 1, 2, 3, q = 1, 2, 3$) there are nine combinations altogether. Therefore, in order to have a good model without going through the long process, prior knowledge of the data pattern and experience play an important part in building the specific model besides autocorrelation and partial autocorrelation. The suggested model for the two series is ARMA(2, 1, 2). The mathematical model is:

$$(1-B)(1-\phi_1 B-\phi_2 B^2)Z_t = (1-\theta_1 B-\theta_2 B^2)a_t \quad \dots 14$$

This model, after estimating its parameters, is subject to diagnostic checking. If the diagnostic checking indicates that the residual autocorrelation is not random then one should look into the autocorrelation function for possible improvement of the model.

Estimation. Using monthly prices for RSS 1 and RSS 2 between January 1970

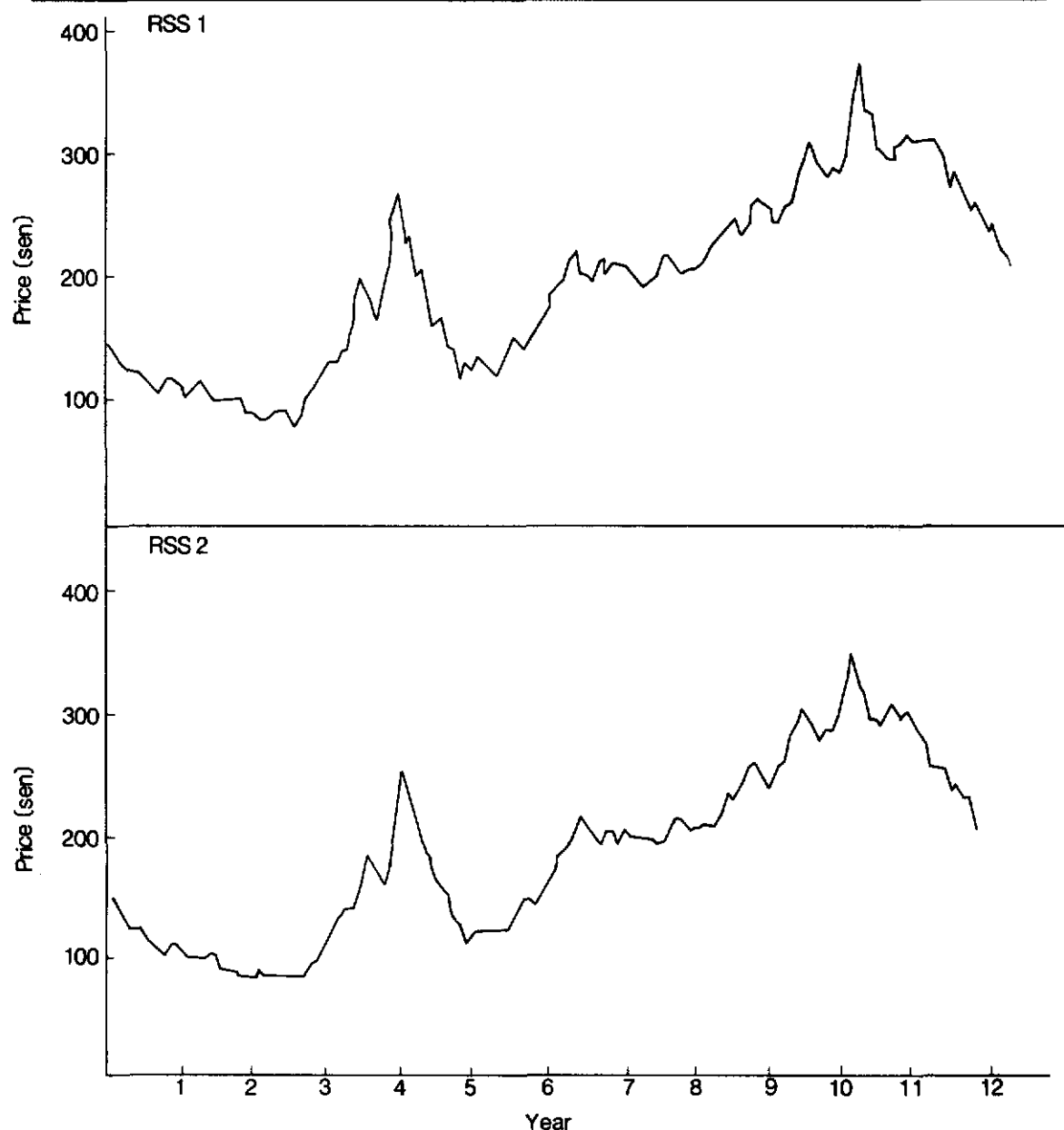


Figure 3. Plots of original data for RSS 1 and RSS 2 prices from 1970-81.

and December 1981 parametric values for Equation 14 were estimated with an available computer routine. For RSS 1,

$$\frac{(1-B)(1 + 0.111B + 0.577B^2)}{(1 + 0.398B + 0.738B^2)} Z_t = a_t \text{ with } \sigma a_t^2 = 0.18269 \dots 15$$

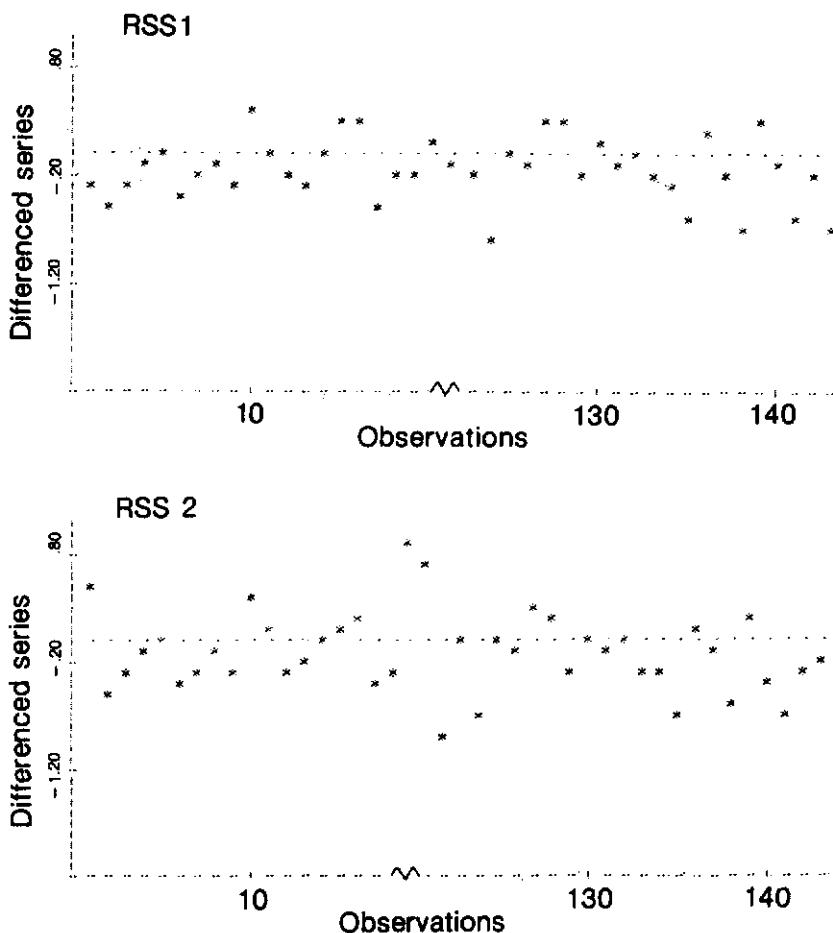


Figure 4. Plot of first degree of regular differencing for RSS 1 and RSS 2.

and for RSS 2;

$$(1-B) (1 + 0.025B + 0.395B^2) Z_t = (1 + 0.407B + 0.590B^2) a_t \text{ with } \sigma a_t^2 = 0.1298 \quad \dots 16$$

To illustrate how the models can be used for forecasting, prices for RSS 1 and RSS 2 were estimated for the next twelve months in 1982. Tables 1 and 2 show the forecasted values, confidence intervals, actual values and percentage errors for the respective series. In these particular samples, the models appeared to predict reasonably well. The average percentage

error forecasting for RSS 1 and RSS 2 for the first eight months of 1982 are 1.11% and 1.68% respectively. The graphic displays for forecasting at one time lead for RSS 1 and RSS 2 are shown in Figures 8 and 9 respectively. The forecast points follow the original data very closely within 95% confidence limits. Whether the models are appropriate or not, however, can be determined in the diagnostic checking step.

Diagnostic checking. After the preliminary models have been identified

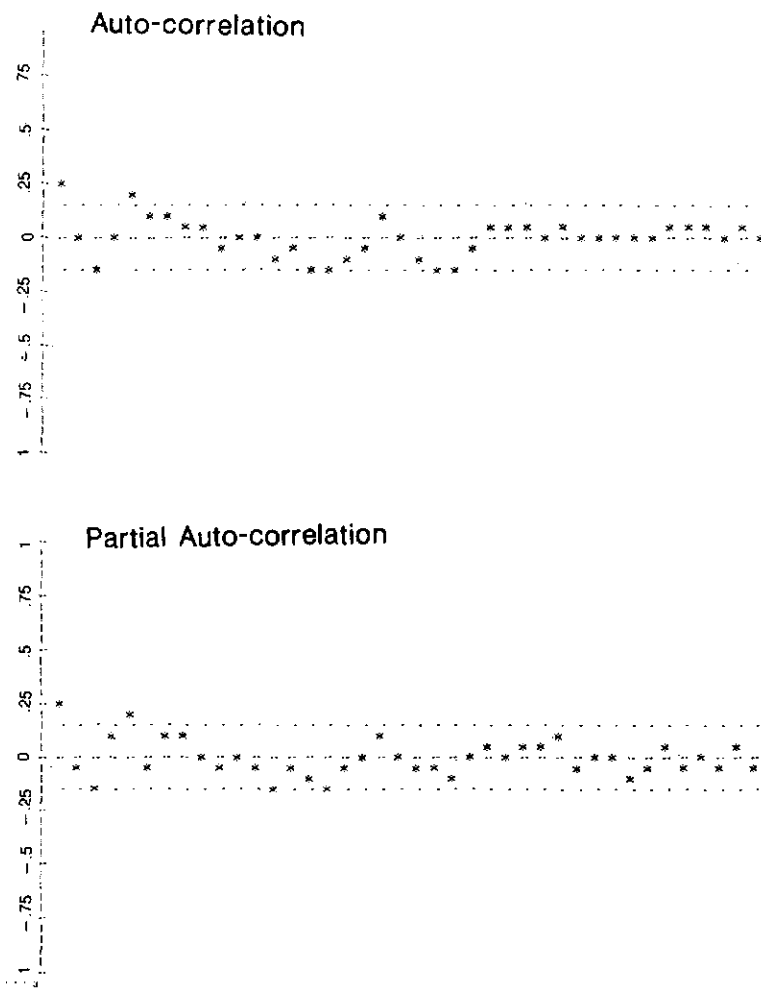


Figure 5. Autocorrelation and partial autocorrelation functions for RSS 1 with two standard error limits.

and estimated, one should examine the models to see whether they are appropriate or not, or whether any improvement can be made. The main objective of the models is to minimise the forecasting errors, a_t , into a set of independent and normally distributed errors with mean zero and constant variance. Therefore, the process of diagnostic checking involves testing whether the residual series is independent and normally distributed

with mean zero and constant variance. Figures 10 and 11 show the residual series of autocorrelation for RSS 1 and RSS 2 series respectively. The dotted lines are 95% confidence intervals. Although a number of residuals do approach the confidence intervals they do not exceed the limits. Therefore, the figures suggest that the residuals are randomly distributed. Tables 3 and 4 are used to check the lack of fit of the models for RSS 1 and RSS 2

LAG	AUTO. STAND		-1	-.75	-.5	-.25	0	.25	.5	.75	1
	CORR.	ERR.									
1	.346	.082						*			
2	.065	.082					*				
3	-.117	.082					*				
4	-.010	.081					*				
5	.161	.081						*			
6	.140	.081						*			
7	.140	.080						*			
8	.019	.080					*				
9	-.002	.080					*				
10	-.047	.079					*				
11	.012	.079					*				
12	.018	.079					*				
13	-.044	.079					*				
14	-.092	.078					*				
15	-.169	.078					*				
16	-.165	.078					*				
17	-.125	.077					*				
18	-.055	.077					*				
19	.050	.077						*			
20	-.076	.076					*				
21	-.205	.076				*					
22	-.181	.076				*					
23	-.114	.075				*					
24	-.001	.075				*					
25	.044	.075					*				
26	.032	.074					*				
27	.064	.074					*				
28	.022	.074					*				
29	.034	.073					*				
30	-.049	.073				*					
31	-.007	.073				*					
32	.002	.073				*					
33	.002	.072				*					
34	.008	.072				*					
35	.041	.071				*					
36	.059	.071				*					
37	.066	.071				*					
38	.048	.070				*					
39	.040	.070				*					
40	-.013	.070				*					

Figure 6. Autocorrelation function for RSS 2 with two standard error limits.

PR-AUT STAND.												
LAG	CORR.	ERR.	-1	-.75	-.5	-.25	0	.25	.5	.75	1	
----- ----- ----- ----- ----- ----- -----												
1	.346	.084					.	.	*			
2	-.062	.084					*.	.				
3	-.137	.084					*.	.				
4	.093	.084					.	.	*			
5	.167	.084					.	.	*			
6	.003	.084					.	*	.			
7	.093	.084					.	.	*			
8	-.017	.084					.	*	.			
9	.005	.084					.	*	.			
10	-.054	.084					.	*	.			
11	.027	.084					.	.	*			
12	-.029	.084					.	*	.			
13	-.082	.084					.	*	.			
14	-.069	.084					.	*	.			
15	-.115	.084					.	*	.			
16	-.108	.084					.	*	.			
17	-.055	.084					.	*	.			
18	-.016	.084					.	*	.			
19	.090	.084					.	.	*			
20	-.105	.084					.	*	.			
21	-.129	.084					*	.	.			
22	.021	.084					.	*	.			
23	-.037	.084					.	*	.			
24	-.001	.084					.	*	.			
25	.060	.084					.	.	*			
26	.032	.084					.	.	*			
27	.113	.084					.	.	*			
28	.024	.084					.	*	.			
29	.041	.084					.	.	*			
30	-.105	.084					*	.	.			
31	-.017	.084					.	*	.			
32	-.034	.084					.	*	.			
33	-.072	.084					.	*	.			
34	-.044	.084					.	*	.			
35	.035	.084					.	.	*			
36	-.033	.084					.	*	.			
37	.022	.084					.	*	.			
38	-.029	.084					.	*	.			
39	.047	.084					.	.	*			
40	-.011	.084					.	*	.			

Figure 7. Partial autocorrelation function for RSS 2 with two standard error limits.

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TABLE 1. FORECASTS FOR RSS 1, ORIGIN AT DECEMBER 1981
AND 95.00% CONFIDENCE LIMITS

Month, 1982	Lower confidence limit	Forecast	Upper confidence limit	Actual	Error (%)
Jan	182.03	205.35	230.08	204.50	0.42
Feb	168.43	205.76	246.83	203.75	0.99
Mar	156.14	204.65	259.71	204.00	0.32
Apr	149.23	204.53	268.54	207.50	1.43
May	144.37	205.19	276.67	205.25	0.03
Jun	138.62	205.18	248.75	204.50	0.33
Jul	133.03	204.80	292.00	200.00	2.43
Aug	128.73	204.85	298.57	199.00	2.94
Sep	124.90	205.06	304.99	—	—
Oct	120.92	205.01	311.18	—	—
Nov	117.16	204.89	317.00	—	—
Dec	113.85	204.94	322.61	—	—
Average	—	—	—	—	1.11

TABLE 2. FORECAST FOR RSS 2, ORIGIN AT DECEMBER 1981
AND 95.00% CONFIDENCE LIMITS

Month, 1982	Lower confidence limit	Forecast	Upper confidence limit	Actual	Error (%)
Jan	175.25	194.45	214.65	194.00	0.23
Feb	163.51	195.78	230.95	191.50	2.23
Mar	151.25	194.18	242.46	191.75	1.27
Apr	144.02	193.69	250.71	192.25	0.75
May	139.30	194.34	258.52	192.00	1.22
Jun	134.31	194.51	265.83	191.25	1.70
Jul	129.33	194.25	272.34	188.75	2.91
Aug	125.09	194.19	278.42	188.25	3.16
Sep	121.37	194.29	284.30	—	—
Oct	117.79	194.32	289.89	—	—
Nov	114.38	194.28	295.20	—	—
Dec	111.22	194.27	300.33	—	—
Average	—	—	—	—	1.68

respectively. The calculation for testing lack of fit is based on the assumption that:

$$Q = n \sum_{i=1}^k r_i^2 ; i = 1, 2, \dots, k , \dots 17$$

where $n = N - d$, is approximately distributed as chi-square distribution with $(k-p-q)$ degree of freedom⁷, if the fitted model is appropriate. The fourth column in *Tables 3* and *4* indicate the levels of significance or probabilities. There is no lag that is significant at either

OBS	DATA	100.00	200.00	300.00	400.00	500.00
96	198.750	:	. X .			
97	202.250	:	. X .			
98	205.500	:	. X .			
99	207.500	:	. X .			
100	207.750	:	. X .			
101	217.500	:	. +* .			
102	235.500	:	. + * .			
103	233.250	:	. *+ .			
104	241.000	:	. +* .			
105	253.750	:	. +* .			
106	259.000	:	. X .			
107	253.250	:	. *+ .			
108	239.000	:	. *+ .			
109	237.500	:	. X .			
110	250.500	:	. +* .			
111	256.750	:	. X .			
112	279.250	:	. + X			
113	292.500	:	. +* .			
114	304.250	:	. X .			
115	292.000	:	. *+ .			
116	284.750	:	. *+ .			
117	281.500	:	. X .			
118	285.750	:	. +* .			
119	289.500	:	. X .			
120	295.500	:	. +* .			
121	332.750	:	. + X			
122	369.250	:	. + * .			
123	328.000	:	. * .			
124	322.500	:	. +* .			
125	293.250	:	. X + .			
126	294.750	:	. *+ .			
127	290.000	:	. X .			
128	300.250	:	. + * .			
129	309.500	:	. X .			
130	303.000	:	. * + .			
131	306.750	:	. +* .			
132	305.000	:	. +* .			
133	304.500	:	. *+ .			
134	299.000	:	. X .			
135	288.500	:	. X .			
136	267.250	:	. * + .			
137	272.500	:	. +* .			
138	267.000	:	. X .			
139	243.500	:	. X + .			
140	254.000	:	. +* .			
141	250.250	:	. *+ .			
142	230.500	:	. X + .			
143	224.250	:	. X .			
144	203.500	:	. * + .			
145	205.349	F :	. 0 .			

Figure 8. Graphic display for forecasting at one time lead for RSS 1.

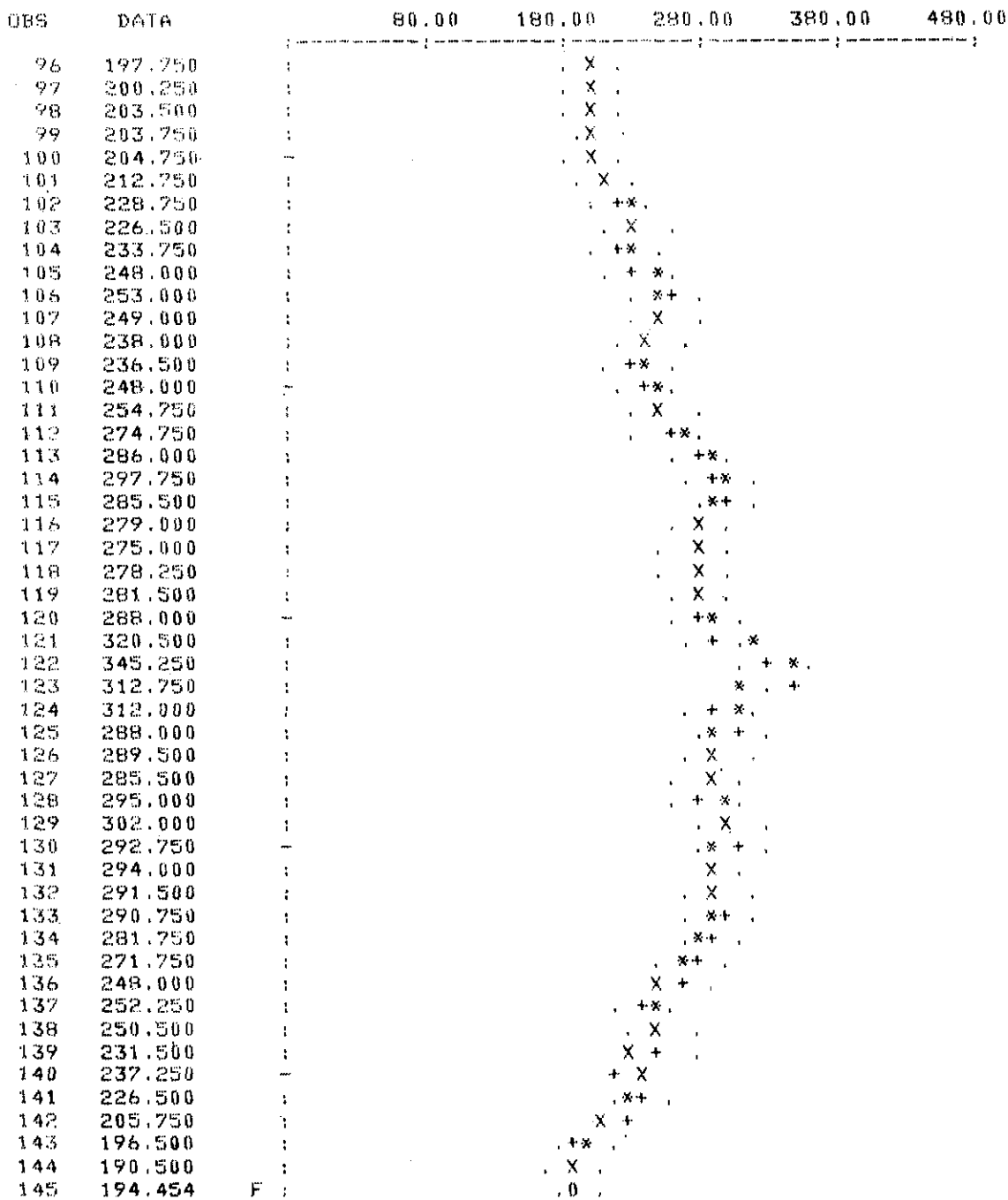


Figure 9. Graphic display for forecasting at one time lead for RSS 2.

LAG	AUTO. CORR.	STAND. ERR.	-1	-.75	-.5	-.25	0	.25	.5	.75	1
1	-.028	.083					*				
2	-.021	.082					*				
3	.010	.082					*				
4	-.016	.082					*				
5	.094	.082						*			
6	.040	.081						*			
7	.108	.081						*			
8	.025	.081					*				
9	.021	.080					*				
10	-.037	.080					*				
11	.006	.080					*				
12	-.009	.079					*				
13	-.090	.079					*				
14	-.013	.079					*				
15	-.094	.078					*				
16	-.121	.078					*				
17	-.069	.078					*				
18	-.071	.077					*				
19	.107	.077						*			
20	-.034	.077					*				
21	-.101	.077					*				
22	-.082	.076					*				
23	-.132	.076					*				
24	-.036	.076					*				
25	.034	.075						*			
26	.047	.075						*			
27	.014	.075					*				
28	.010	.074					*				
29	.084	.074						*			
30	-.066	.074					*				
31	.027	.073						*			
32	.018	.073					*				
33	-.001	.073					*				
34	-.019	.072					*				
35	.038	.072						*			
36	.044	.071						*			
37	.050	.071						*			
38	-.050	.071					*				
39	.064	.070						*			
40	.019	.070					*				

Figure 10. Residual autocorrelation function for RSS 1 with two standard error limits.

LAG	AUTO. CORR.	STAND. ERR.	-1	-.75	-.5	-.25	0	.25	.5	.75	1
1	.004	.083					*				
2	-.014	.082					*				
3	.027	.082					1*				
4	-.016	.082					*				
5	.096	.082					1 *				
6	.048	.081					1*				
7	.119	.081					1 *				
8	.019	.081					*				
9	-.001	.080					*				
10	-.062	.080					*1				
11	.026	.080					1*				
12	.016	.079					*				
13	-.035	.079					*1				
14	-.043	.079					*1				
15	-.145	.078					* 1				
16	-.064	.078					*1				
17	-.079	.078					* 1				
18	-.088	.077					* 1				
19	.093	.077					1 *				
20	-.061	.077					*1				
21	-.167	.077					* 1				
22	-.079	.076					* 1				
23	-.081	.076					* 1				
24	.000	.076					*				
25	.038	.075					1*				
26	.008	.075					*				
27	.048	.075					1*				
28	.001	.074					*				
29	.045	.074					1*				
30	-.071	.074					*1				
31	.030	.073					1*				
32	-.000	.073					*				
33	.004	.073					*				
34	-.006	.072					*				
35	.025	.072					1*				
36	.065	.071					1*				
37	.014	.071					*				
38	.000	.071					*				
39	.073	.070					1*				
40	.004	.070					*				

Figure 11. Residual autocorrelation for RSS 2 with two standard error limits.

TABLE 3. DIAGNOSTIC CHI-SQUARE FOR RESIDUAL SERIES RSS 1

Lag	Chi-square	Df	Probability
6	1.75	2	0.4164
12	3.91	8	0.8655
18	10.57	14	0.7194
24	18.73	20	0.5395
30	21.46	26	0.7176
36	22.36	32	0.8973
40	24.21	36	0.9329

TABLE 4. DIAGNOSTIC CHI-SQUARE FOR RESIDUAL SERIES RSS 2

Lag	Chi-square	Df	Probability
6	1.87	2	0.3918
12	4.81	8	0.7775
18	11.57	14	0.6405
24	20.48	20	0.4281
30	22.44	26	0.6643
36	23.56	32	0.8598
40	24.66	36	0.9235

5% or 10% level (*i.e.* $\alpha = 0.05$ or $\alpha = 0.10$). Thus the residual series of autocorrelation and chi-square tests cast no doubt that the models are appropriate.

DISCUSSION AND VALIDITY OF THE MODELS

The models that are obtained and presented in this paper are univariate stochastic models. This simple approach cannot be expected to produce very accurate forecasts over long-term periods but they may be useful for short-term forecasting, and these models are important for the following reasons⁸:

- It may be impossible to obtain variables related to the variable being forecast, leaving univariate models as a choice.
- The development of univariate models provides a 'yardstick'

with which more sophisticated models can be compared whenever the related variables may be used to improve the accuracy of the forecasts.

- Univariate models serve as a tool for screening data during the early stages for an analyst if the cause of large residuals can be identified.

The models developed are not ultimate models. The long-term forecasts for rubber prices may need to consider a few related substitutes, demand for rubber products, *etc.* Yet, the variables related to dependent variables can be incorporated into a multivariate transfer function which is equivalent to the simultaneous equation system.

We observe that the 95% confidence limits in *Tables 1* and *2* become wider as the time lead increases. This is a reflection of the increase in forecast error variance as the time lead increases. One may suggest that updating the parameter estimates as new data become available usually leads to better forecasts. Another way of obtaining better forecasts is by updating the forecast to a new origin ($t+1$) whenever a new deviation is available.

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